

系所組：機械工程學系數位機電碩士班乙組、丙組

日期節次：102 年 3 月 15 日第 1 節 9:00~10:30

科目：工程數學

Problem1(20%)

(a) The Laplace transformation is limited to what kind of Equation?

(b) Please Solve the Equations:

$$4y'' + (\pi)^2 y = 0, y(0) = 2, y'(0) = 0$$

$$y'' - 4y' + 3y = 2t - 8/3, y(0) = 0, y'(0) = -16/3$$

Problem2(20%)

please use the matrix of A to find the answer of(a) and (b)

(a) $A = \begin{bmatrix} -2 & -1 \\ 5 & 2 \end{bmatrix}$ (Matlab Matrix expression) find eigenvalues of A?

(b) $A = \begin{bmatrix} 2 & 1 & 0 \\ 3 & 2 & 0 \\ 0 & 0 & 4 \end{bmatrix}$ (Matlab Matrix expression), if $\lambda = 4$ is one of the eigenvalues, Please find the two others ?

Problem3(20%)

(a) Please find the inverse of b when $b = \begin{bmatrix} 2 & 3 & 1 \\ 1 & 2 & 3 \\ 3 & 1 & 2 \end{bmatrix}$

(b) $d = \begin{bmatrix} d_{11} & 0 & 0 & 0 & \dots \\ 0 & d_{22} & 0 & 0 & \dots \\ \dots & \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & d_{nn} \end{bmatrix}$, please find the inverse of a diagonal matrix d=?

Problem4 (20%)

Calculate the transpose of matrix A and B--- A^T and B^T , please

$A = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$, $B = \begin{bmatrix} 3 & 3 & 3 \\ 2 & 2 & 2 \end{bmatrix}$, then $AB = ?$ Find B^T and A^T , then find AB^T , $B^T A^T$, what is your conclusion?

Problem5(20%)

Solve the linear system:

$$3x_1 - x_2 + 2x_3 = 12$$

$$x_1 + 2x_2 + 3x_3 = 11$$

$$2x_1 - 2x_2 + x_3 = 2$$

Using Gaussian Elimination and back substitution, (hint: find the augmented matrix first)